Closing Tue, Apr. 7: 12.1, 12.2, 12.3 Closing Thu, Apr. 9: 12.4(1)(2),12.5(1)

126: Calculus III - Dr. Andy Loveless

12.1 Intro to 3D

Entry Task: How can you tell if a point (x,y,z) in \mathbb{R}^3 is on...

- 1. ...the xy-plane?
- 2. ...the yz-plane?
- 3. ...the z-axis?
- 4. ...the x-axis?
- 5. ...the origin?

Observations

Basic Planes

xy-plane $\Leftrightarrow \{(x, y, z) \mid z = 0\} \Leftrightarrow z = 0$ yz-plane $\Leftrightarrow \{(x, y, z) \mid x = 0\} \Leftrightarrow x = 0$ xz-plane $\Leftrightarrow \{(x, y, z) \mid y = 0\} \Leftrightarrow y = 0$

Basic Lines

x-axis $\Leftrightarrow \{(x, y, z) \mid y = 0 \text{ and } z = 0\}$ y-axis $\Leftrightarrow \{(x, y, z) \mid x = 0 \text{ and } z = 0\}$

z-axis $\Leftrightarrow \{(x, y, z) \mid x = 0 \text{ and } y = 0\}$

Distances: The distance (in a straight line) between two points in \mathbb{R}^3 is

$$\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2 + (z_2 - z_1)^2}$$

How far is (1,3,4) from...

- 1. ...the origin?
- 2. ...the xy-plane?
- 3. ...the x-axis?

Homework Hints

There is a way to answer the following questions using only the distance formula:

Given three points

 $A(a_1, a_2, a_3), B(b_1, b_2, b_3), C(c_1, c_2, c_3)$

- 1. Are the points on the same line?
- 2. Do the points form a right triangle?

Spheres (HW 12.1/6-16)

The equation of all points (x, y, z) on a sphere (*i.e.* the outer shell of a ball) centered at (h, k, l) with radius r is

$$(x-h)^2 + (y-k)^2 + (z-l)^2 = r^2$$

Example: Find the equation of the sphere that has its lowest point at (0,0,1) and its highest point at (0,0,5).

Example:

What if it was the *xy*-plane?

Describe the intersection of the sphere $x^2 + y^2 + (z - 3)^2 = 4$

and the *xz*-plane.

Example: Find the center and radius of the sphere

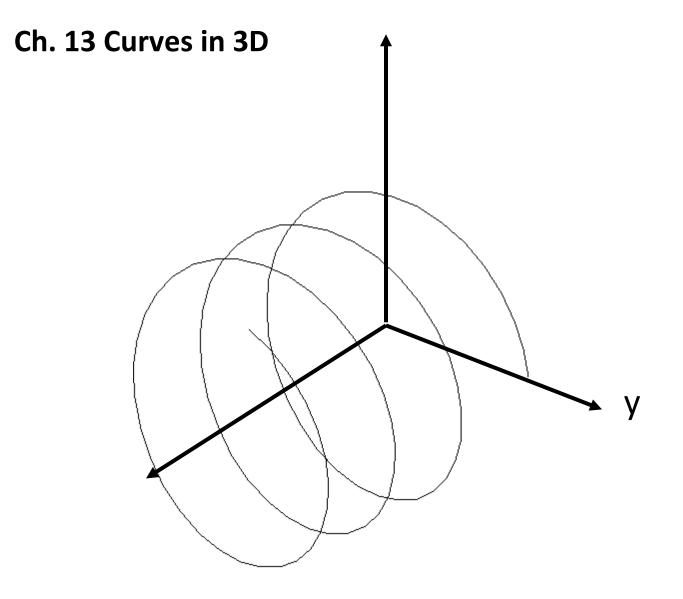
 $2x^2 + 2y^2 + 2z^2 = 26 + 12x$

What we will do in this course:

- Ch. 12 Vectors and 3D Basics (vector operations, lines, planes)
- Ch. 10/13 2D and 3D Curves
 (parametric, polar, dis/vel/acc)
- Ch. 14 Analyzing Surfaces
 (partials, tangents, max/min)
- Ch. 15 Volumes under Surfaces (double Integrals)
- 5. Taylor Notes Taylor Polynomials and Taylor Series

How to get help: First, work ahead on homework; pretend the closing date is actually two days early.

- Ask questions on discussion board!!!!
- 2. Ask questions when your TA is on Zoom or discussion board.
- 3. Ask questions during live-stream lectures.
- 4. Email your TA or me.
- 5. Form Zoom study groups with classmates.
- 6. Use my free online resources



Ch. 14/15 Surfaces in 3D

